

Special girder bridges

Truss bridges

Cantilever-constructed bridges

Introduction / first cantilever-constructed bridges



General observations



Design



Camber



Construction

Truss bridges

General Observations



Types and examples



Design



Skew bridges

...



Curved bridges

...

Introduction



Analysis



Design



Particularities of steel bridges

Special girder bridges

Truss bridges

General observations

Truss bridges – General observations

Advantages and drawbacks of truss bridges

Truss bridges are **structurally very efficient**: The top and bottom chords, connected by truss members rather than a solid web, provide

- **high bending stiffness and strength** at
- **low self-weight**

Trusses are in fact close to a pure **stringer cross-section** (see superstructure / structural efficiency).

For these reasons, truss bridges found **widespread application in the 19th and early 20th century**, when steel was expensive and scarce, and **minimising material consumption** was therefore a main concern of bridge designers.



Truss bridges – General observations

Advantages and drawbacks of truss bridges

However, the **joints** connecting the truss members, which may be

- **welded** (common in Europe),
- **bolted** (common in US), or
- **riveted** (common in historic bridges)

need to be carefully designed and detailed, and require a **significant amount of labour**.

Hence, truss bridges may be **economical** today merely for **larger spans**, where the corresponding cost is compensated by savings due to the structural efficiency. Even for long spans, however, other bridge types (e.g. cable stayed bridges) are often less expensive today.

This is the main reason why **few truss bridges** were built in the last decades.



Truss bridges – General observations

Advantages and drawbacks of truss bridges

Another reason why few modern truss bridges were built is their appearance. Trusses are

- **transparent**, yet often only in frontal view, but
- require **more depth** than other girder types (see design)
- may appear **old-fashioned**, particularly trusses with bolted connections (gusset plates) and through trusses

Example: Few people would bet that the Milton Bridge (photo) was **built only in 2015**, even if the bridge ends, with vertical end posts, differ from typical solutions used historically.

This solution was chosen here since the bridge replaced an existing through truss bridge with shorter span.



Truss bridges – General observations

Advantages and drawbacks of truss bridges

Further disadvantages of truss bridges, limiting their use in modern bridge design, are:

- **High maintenance demand** due to large exposed surfaces, particularly in through and pony trusses not protected by the deck
- Typically trusses are isostatic, such that all individual members are “**fracture critical**”: Failure of one member will lead to a global collapse.

The photos show the I35-W Mississippi bridge, which collapsed in 2007 during resurfacing works. Presumably, failure of undersized gusset plates triggered the collapse (construction equipment and up to 5 cm concrete/pavement added since original construction caused high loads).

Note that **redundancy** can be achieved by providing extra trusses running in parallel, such that one truss may fail without causing global collapse. However, this causes high extra cost.



Special girder bridges

Truss bridges

Types and examples

Truss bridges – Types and examples

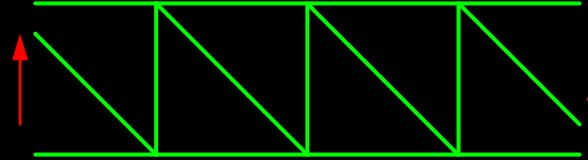
Types of trusses

Trusses can be classified according to the **configuration of the (main) truss members**.

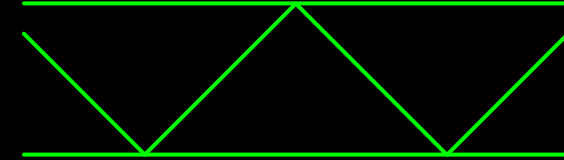
This slide compiles the most important truss layouts. Note that some designations are subject to regional preferences.

In some cases, **secondary members** are introduced to reduce buckling lengths of compression members and/or reduce the span of the chord carrying the deck (see also next slide).

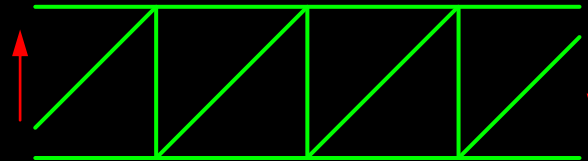
Pratt truss / Ständerfachwerk (Zugdiag.)



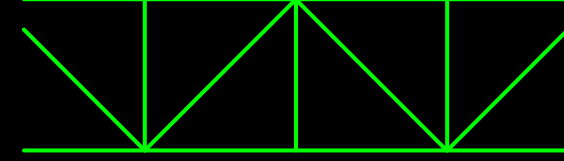
Warren truss / (ständerloses) Strebenfachwerk



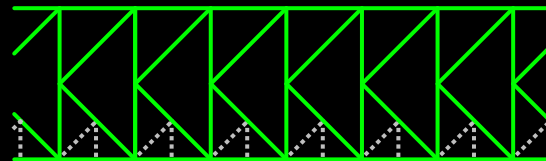
Howe truss / Ständerfachwerk (Druckdiag.)



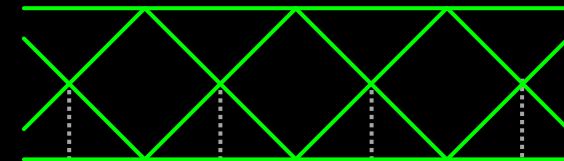
Modified Warren truss / Strebenfachwerk



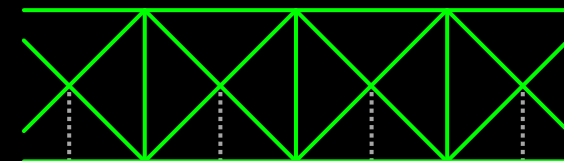
K-truss / K-Fachwerk



Brown (Diamond) truss / Rhombenfachwerk



Long truss / Kreuzfachwerk



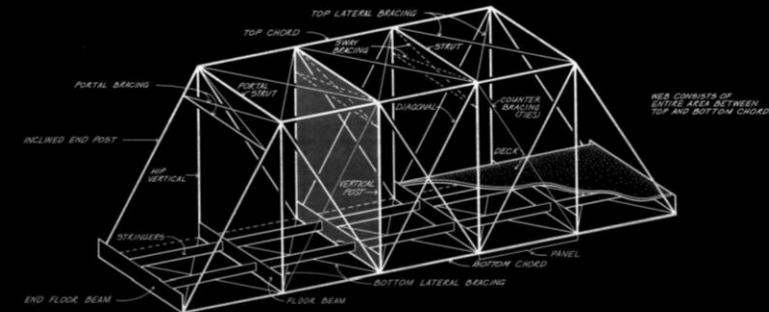
[Illustrations adapted from
P. Marti, Theory of Structures,
Section 11.3: Trusses]

Truss bridges – Types and examples

Types of trusses

More examples of truss types and designations, used mainly in the U.S.

(nomenclature merely of historical interest)



TRUSSES

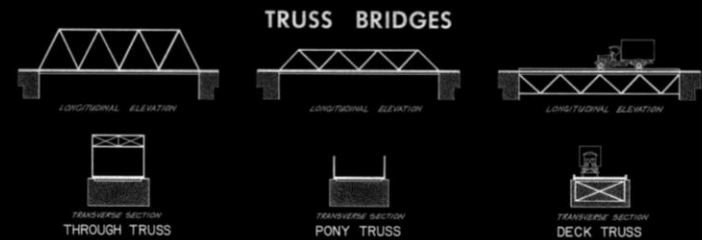
A STUDY BY THE
HISTORIC AMERICAN ENGINEERING RECORD

A TRUSS IS COMPOSED OF STRUCTURAL MEMBERS JOINED TOGETHER WITH PINNED OR CURVED CONNECTIONS. THE MAIN PURPOSE OF MEMBERS MAY BE EITHER STIFF STAYS, PART OF TWO RIGID BARS, OR THE SEGMENTATION OF THESE MEMBERS. THE DETERMINING THE SPACING TYPE.

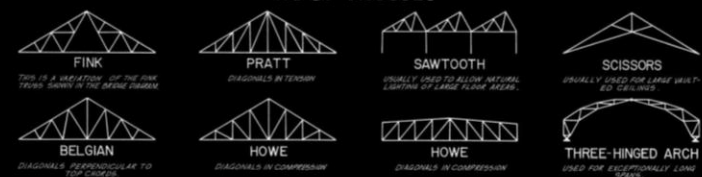
STRUCTURAL MEMBERS RESIST FORCES IN TWO PRINCIPAL WAYS — COMPRESSION AND TENSION. HEAVY LOADS INCREASED MAY RESIST BOTH COMPRESSION AND TENSION. FORCES THAT DO NOT EXIST ON ONLY TENSION AND THESE CHARACTERISTICS ARE MAJOR CLUES IN TRUSS IDENTIFICATION. NOTE THAT THE MAIN STRUCTURAL MEMBERS OF A TRUSS, WHEN AS REPRESENTED BY THIN DRAWING LINES, INDICATE HOW THEY ARE DETERMINED BY THIN DRAWING LINES. THESE COUNTER BRACES (INDICATED BY BOLD LINES) INDICATE HOW THEY ARE DETERMINED BY THIN DRAWING LINES. INDICATING THE STRUCTURAL OUTLINE OF THE TRUSS IS QUESTION WITH THE DIAGRAM IS NOT RESEMBLED CARRY TO MAKE SURE THE ARRANGEMENT OF HEAVY COMPRESSION AND LIGHT TENSION MEMBERS IS COMPATIBLE WITH THE DIAGRAM. IF THERE IS AGREEMENT, THEN THE BASIC TRUSS TYPE IS IDENTIFIED.

THE SHEET OF TRUSS DIAGRAMS PRESENTS ONLY THE STANDARD FORMS OF THE MOST COMMON TRUSSES. THERE ARE ALSO MANY VARIATIONS THAT DO NOT FALL INTO EASILY DEFINED CATEGORIES. IN SUCH CASES IDENTIFICATION MUST BE MADE AS CLOSELY AS POSSIBLE IN TERMS OF THE STANDARD DESIGN. ADDITIONALLY, DIFFERENT FROM THE ORIGINAL TENSION MEMBERS FOLLOWING COMPRESSION MEMBERS AND VICE VERSA. ASSUMING A TRUSS IS NOT REPRESENTED ON THE DIAGRAM, CHECK TO SEE IF IT IS AN INVERTED FORM.

MOST BRIDGE TRUSSES ARE OF THREE BASIC TYPES. IN THE FIRST AND SECOND CASES, THE TRUSS IS IDENTIFIED WITH THE BASIC TYPE. IN THE THIRD CASE, THE TRUSS IS IDENTIFIED WITH THE BASIC TYPE. IN THE THIRD CASE, THE TRUSS IS IDENTIFIED WITH THE BASIC TYPE.



ROOF TRUSSES



<p>KING POST (WOOD) A TRADITIONAL TRUSS TYPE WITH ITS DESIGN IN THE MIDDLE ARCS. LENGTH: 20-40 FEET 8-12 METERS</p>	<p>PRATT 1844 - 20TH CENTURY DIAGONALS IN TENSION, VERTICALS IN COMPRESSION. VERTICALS FOR TOP JOINTS ADJACENT TO INCLINED END RAILS. LENGTH: 30-50 FEET 9-15 METERS</p>	<p>BALTIMORE (PETIT) 1871 - EARLY 20TH CENTURY A PRATT WITH SUB-STRUTS A PRATT WITH SUB-STRUTS LENGTH: 25-400 FEET 7.5-120 METERS</p>	<p>WARREN 1840 - 20TH CENTURY TRIANGULAR IN OUTLINE THE DIAGONALS CARRY BOTH COMPRESSION AND TENSION. VERTICALS SERVE AS BRACING FOR THE TRIANGULAR SYSTEM. LENGTH: 50-400 FEET 15-120 METERS</p>
<p>QUEEN POST (WOOD) A LENGTHENED VERSION OF THE KING POST. LENGTH: 20-30 FEET 6-24 METERS</p>	<p>PRATT HALF-HIP LATE 19TH - EARLY 20TH CENTURY A PRATT WITH INCLINED END RAILS THAT DO NOT HORIZONTALLY EXTEND THE LENGTH OF A FULL PANEL. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>PENNSYLVANIA (PETIT) 1871 - EARLY 20TH CENTURY A PRATT WITH SUB-STRUTS A PRATT WITH SUB-STRUTS LENGTH: 25-400 FEET 7.5-120 METERS</p>	<p>WARREN WITH VERTICALS MID 19TH - 20TH CENTURY DIAGONALS CARRY BOTH COMPRESSION AND TENSION. VERTICALS SERVE AS BRACING FOR THE TRIANGULAR SYSTEM. LENGTH: 50-400 FEET 15-120 METERS</p>
<p>BURR ARCH TRUSS 1804 - LATE 19TH CENTURY (WOOD) COMBINATION OF A WOODEN ARCH WITH A MULTIPLE KING POST (ARCH ALSO COMBINED WITH LATER WOODEN TRUSSES). LENGTH: 30-150 FEET 9-45 METERS</p>	<p>TRUSS LEG BEDSTEAD LATE 19TH - EARLY 20TH CENTURY A PRATT WITH VERTICAL END POSTS INCLINED IN THEIR FOUNDATIONS. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>LENTICULAR (PARABOLIC) 1870 - EARLY 20TH CENTURY A PRATT WITH BOTH TOP AND BOTTOM CHORDS PARABOLICALLY CURVED OVER THEIR ENTIRE LENGTH. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>DOUBLE INTERSECTION WARREN MID 19TH - 20TH CENTURY STRUCTURE IS INDETERMINATE. MEMBERS ACT IN BOTH COMPRESSION AND TENSION. THE TRIANGULAR WEB SYSTEMS ARE SUPERIMPOSED UPON EACH OTHER WITH DIFFERENT ORIENTATIONS. LENGTH: 15-400 FEET 4.5-120 METERS</p>
<p>TOWN LATTICE 1810 - LATE 19TH CENTURY (WOOD) A SYSTEM OF INTERLACING DIAGONALS WITH NO VERTICAL OR HORIZONTAL STRUTS. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>PARKER MID-LATE 19TH - 20TH CENTURY A PRATT WITH A POLYGONAL TOP CHORD. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>GREINER 1844 - EARLY 20TH CENTURY PRATT TRUSS WITH THE DIAGONALS REPLACED BY AN INVERTED BUSHING TRUSS. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>PEGRAM 1841 - EARLY 20TH CENTURY A HYBRID BETWEEN THE WARREN AND PRATT TRUSSES. UPPER CHORDS ARE ALL OF EQUAL LENGTH. LENGTH: 15-400 FEET 4.5-120 METERS</p>
<p>HOWE 1840 - 20TH CENTURY (WOOD, VERTICALS OF METAL) DIAGONALS IN COMPRESSION, VERTICALS IN TENSION. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>CAMELBACK LATE 19TH - 20TH CENTURY A PARKER WITH A POLYGONAL TOP CHORD OF EXACTLY FIVE SLOPES. LENGTH: 100-300 FEET 30-90 METERS</p>	<p>DOUBLE INTERSECTION PRATT 1841 - 20TH CENTURY (WHIPPLE, WHIPPLE-MURPHY, LITTLE) AN INCLINED END POST PRATT WITH DIAGONALS THAT EXTEND ACROSS TWO PANELS. LENGTH: 70-300 FEET 21-90 METERS</p>	<p>POST 1845 - LATE 19TH CENTURY A HYBRID BETWEEN THE WARREN AND THE DOUBLE INTERSECTION PRATT. LENGTH: 100-300 FEET 30-90 METERS</p>
<p>BOWSTRING ARCH-TRUSS 1840 - LATE 19TH CENTURY A TIED ARCH WITH THE DIAGONALS SERVING AS BRACING AND THE VERTICALS SUPPORTING THE ARCH. LENGTH: 30-150 FEET 9-45 METERS</p>	<p>CAMELBACK LATE 19TH - EARLY 20TH CENTURY A POLYGONAL TRUSS WITH A POLYGONAL TOP CHORD TO CARRY THE ENTIRE LOAD. LENGTH: 100-300 FEET 30-90 METERS</p>	<p>SCHWEDLER LATE 19TH CENTURY A DOUBLE INTERSECTION PRATT POSITIONED IN THE CENTER OF A PARKER. LENGTH: 100-300 FEET 30-90 METERS</p>	<p>BOLLMAN 1851 - MID-LATE 19TH CENTURY (RAIL) VERTICALS IN COMPRESSION, DIAGONALS IN TENSION. DIAGONALS RUN FROM END POSTS TO EACH PANEL POINT. LENGTH: 15-100 FEET 4.5-30 METERS</p>
<p>WADDELL "A" TRUSS LATE 19TH - EARLY 20TH CENTURY A LENGTHENED VERSION OF THE KING POST TRUSS. USUALLY MADE OF METAL. LENGTH: 25-75 FEET 8-23 METERS</p>	<p>KELLOGG LATE 19TH CENTURY A VARIATION ON THE PRATT WITH ADDITIONAL DIAGONALS. ENDING FROM THE CENTER OF THE LOWER CHORDS. LENGTH: 75-150 FEET 23-45 METERS</p>	<p>K-TRUSS EARLY 20TH CENTURY TO CARRY LOADS OF THE DISJOINTED OUTLINE OF THE STRUCTURAL MEMBERS. LENGTH: 200-300 FEET 60-90 METERS</p>	<p>FINK 1841 - MID-LATE 19TH CENTURY (RAIL) VERTICALS IN COMPRESSION, DIAGONALS IN TENSION. LONGEST DIAGONAL RUN FROM END POSTS TO EACH PANEL POINT. LENGTH: 15-100 FEET 4.5-30 METERS</p>
<p>WICHERT</p>	<p>TRUSSES A STUDY BY THE HISTORIC AMERICAN ENGINEERING RECORD</p>	<p>STEARNS</p>	

Truss bridges – Types and examples

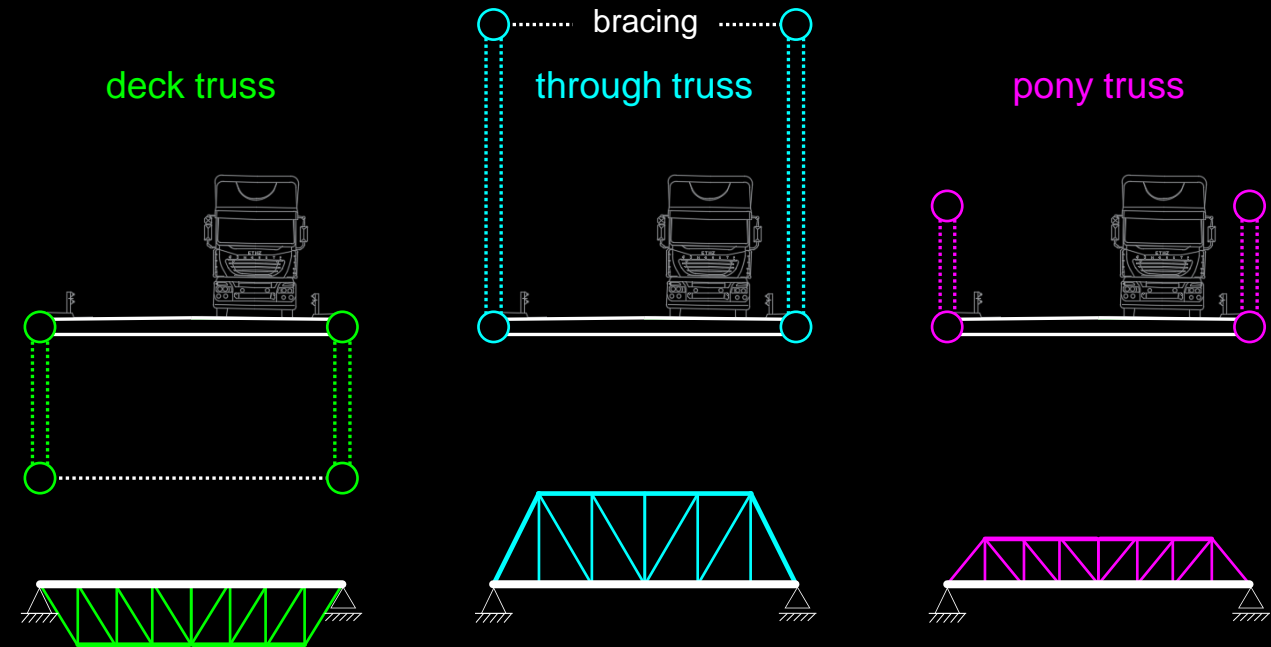
Types of truss bridges

Truss bridges are usually girder bridges. Apart from the truss type, they can be classified according to the **arrangement of top and bottom chords** respective to the deck:

- **Deck truss bridge:** Truss(es) below the deck
- **Through truss bridge:** Trusses running along deck sides, bottom chords at deck level, connection of top chords above deck
- **Pony truss bridge:** As through truss, but with reduced height and hence, without top chord connection

Many truss bridges have **parallel chords**, i.e. a constant depth (“Parallelträger”), though end posts are often inclined (“Trapezträger”).

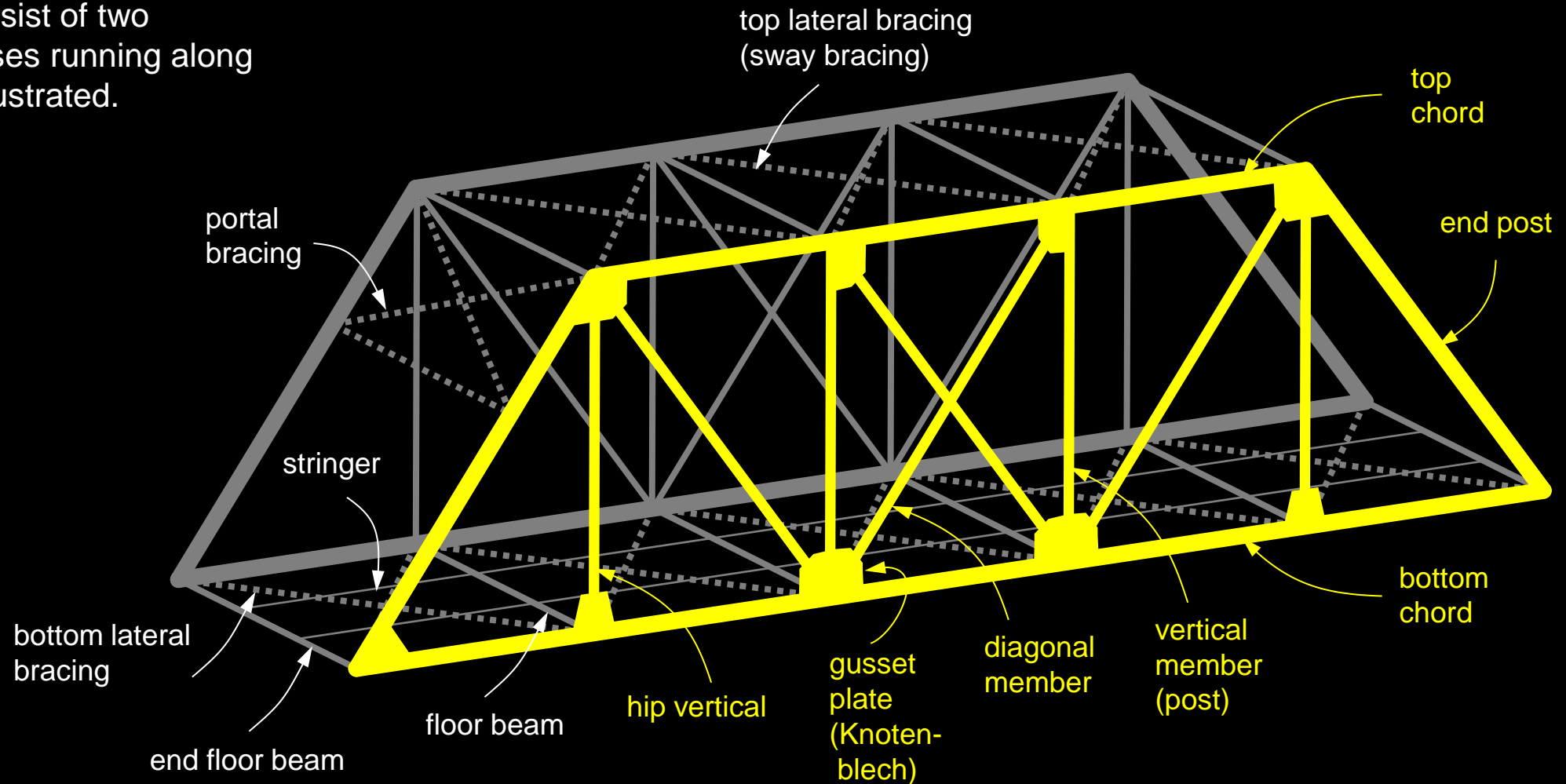
Variable depth trusses are often structurally more efficient, but their production is more demanding (varying joint geometries).



Truss bridges – Types and examples

Truss bridge components (nomenclature)

Many truss bridges consist of two longitudinal, plane trusses running along the bridge edges, as illustrated.



Truss bridges – Types and examples

Truss bridge examples

On this and the following slides, typical examples of parallel chord trusses and variable depth trusses are shown.

Common truss types with **parallel chords**:

- **Pratt truss / Ständerfachwerk (mit Zugdiagonalen):**
Reduced buckling length of compression members (Rheinbrücke Eglisau, 1897)
- **Howe truss / Ständerfachwerk (mit Druckdiagonalen):**
Used mainly for timber trusses due to simpler vertical tension members (Cascadia Park Bridge, 1928).

Note: As usual in timber bridges, many Howe trusses are covered. The system is often combined with additional, diagonals (X-bracing with double compression diagonals, single tension diagonals and vertical tension posts).



Truss bridges – Types and examples

Truss bridge examples

Common truss types with **parallel chords** (continued):

- **Warren truss / ständerloses Strebenfachwerk:** Simple, clean geometry, unpretentious appearance, low weight, equal member length if triangles are equilateral (Itztalbrücke, 2005).
- **K-truss:** Reduced buckling length of bracing members (Speers railroad bridge, 1931).



Truss bridges – Types and examples

Truss bridge examples

Common truss types with **parallel chords** (continued):

- **Long truss / Kreuzfachwerk:** Crossed diagonals and vertical posts (Saaneviadukt Gümmenen, 1901).
- **Brown truss / Rhombenfachwerk:** Crossed diagonals without vertical posts (Saaneviadukt Gümmenen, 2021).

Note: The replacement of the Saaneviadukt Gümmenen is remarkable, as the truss panel length is varied along with the shear forces – an innovative design based on a truss type patented in 1846.



Truss bridges – Types and examples

Truss bridge examples

Common **variable depth** truss types:

- **Parker truss / (Halb-)Parabelträger:** Variable depth truss, one chord aligned with deck
(top: Lake Oswego Bridge, Oregon, 1910, Parker Truss;
bottom: SOB Sitterviadukt, St. Gallen, 1910, inverted Parker Truss)

Parker trusses are strictly speaking only those having a Pratt bracing. In the U.S., depending on the layout, many different names exist, such as «Pennsylvania» or «Petit» (Parker provided with sub-struts or ties) and “Camelback» (Parker where top chord has exactly five different inclinations). See behind for more examples.

In German, Parker trusses are sometimes also referred to as “Schwedlerträger” (although Schwedler’s original design, intending to avoid compression in the diagonals, involved a downward kink in the top chord at midspan)



Truss bridges – Types and examples

Truss bridge examples

Common **variable depth** truss types:

- **Lenticular truss / Pauliträger:** Variable depth truss, both chords curved, typically Pratt or cross bracings (top: first SBB Aarebrücke Brugg, 1875; bottom: Royal Albert Bridge, 1859).

Note that this layout is inefficient since neither of the chords is aligned with the deck. Few bridges were built for this reason.



Truss bridges – Types and examples

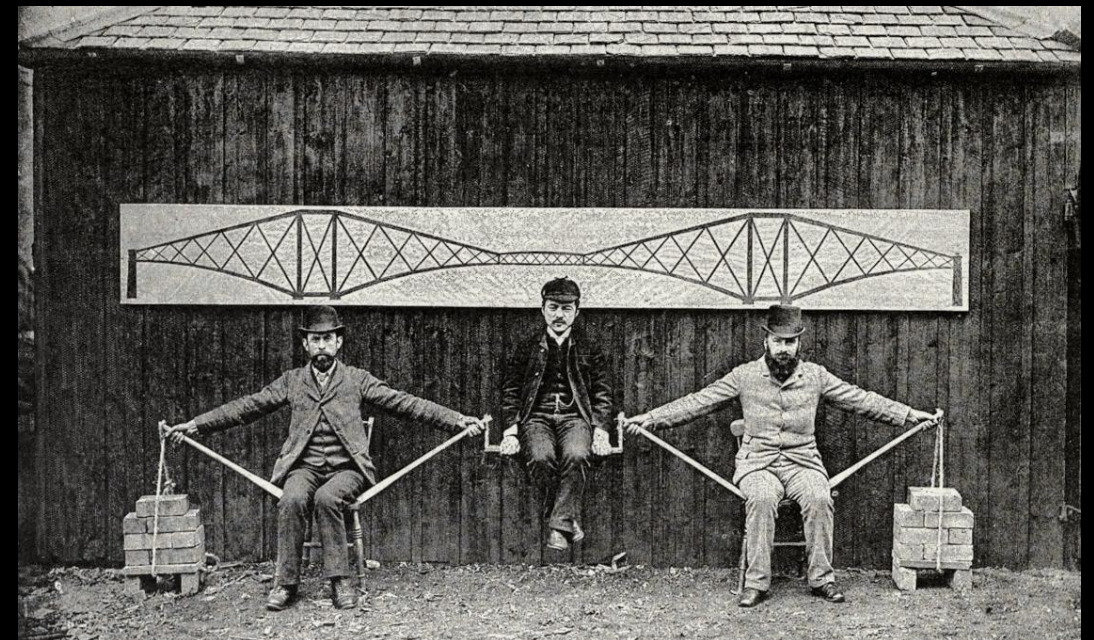
Truss bridge examples

Common **variable depth** truss types:

- **Cantilever truss:** Variable depth trusses, with maximum depth over piers to enable cantilever construction of the bridge.

This typology is very useful particularly for crossing obstacles without temporary supports.

Two cantilever truss bridges held the world span record (which is usually the domain of suspension bridges) from 1890-1929: The Forth Bridge, designed by John Fowler and Benjamin Baker (1890, span 520 m), shown on this slide, and the Québec Bridge (1918, span 549 m), see next slide.



Truss bridges – Types and examples

Truss bridge examples

Common **variable depth** truss types:

The Québec Bridge was rebuilt 1918, after having collapsed in construction 1907.

This was one of the most tragic bridge construction accidents in history, killing 75 workers. Although it was known before that the steel weight had been substantially underestimated in the design, construction had not been stopped in time.

In addition, the centre section of the reconstructed bridge fell when lifted first in 1916, killing another 13 workers.



Truss bridges – Types and examples

Truss bridge examples

Common **variable depth** truss types:

Similar bridges were built worldwide. A noteworthy example is the Rabindra Setu / Howrah Bridge in Kolkata (1942).

This cantilever truss has a suspended deck and is one of the busiest bridges today.



Truss bridges – Types and examples

Truss bridge examples

Uncommon yet interesting truss types:

- **Fink truss / Fink'scher Träger:** Multiple overlapping diagonal members and vertical posts (puente de Fierro / Bolívar, 1882).
- **Inverted Fink trusses** have seen a revival for footbridges over the past years, due to their expressive character (Frank Gehry Bridge, 2015).



Truss bridges – Types and examples

Truss bridge examples

Uncommon yet interesting truss types (continued):

- **Wichert truss**: Isostatic truss with continuity at intermediate supports, thanks to a rhomboidal truss layout over the piers (Homestead Grays bridge, 1936).

Note: Understanding the behaviour of Wichert trusses is not as intuitive as for other trusses – see e.g. D. Steinman, The Wichert Truss, 1932.
- The **Wichert system** has also been used for concrete girders in soft soil, with concrete hinges (Smithy Wood Footbridge, 1965).



Truss bridges – Types and examples

Truss bridge examples

Vierendeel “trusses” (no trusses, though sometimes the term is used: they would be unstable with pin-connected joints).

- **Vierendeel girder**: Frame made up of parallel chords and vertical posts, with rigid connections (transfer of bending moments), but no diagonal members (Gustav Heinemann Brücke 2005).

Vierendeel girders are flexible since global shear forces contribute significantly to the deflections → structurally inefficient, even higher depth required than for “real” trusses. Suitable primarily for short span and/or footbridges (bridge shown is provided with vibration absorbers).

- **Vierendeel arch**: Vierendeel girder with curved top chord. May also be interpreted as tied arch bridge with stiff hangers (Gellik Railway Bridge, 1934). Vierendeel arches are more efficient than Vierendeel girders, see Arch Bridges chapter.



Truss bridges – Types and examples

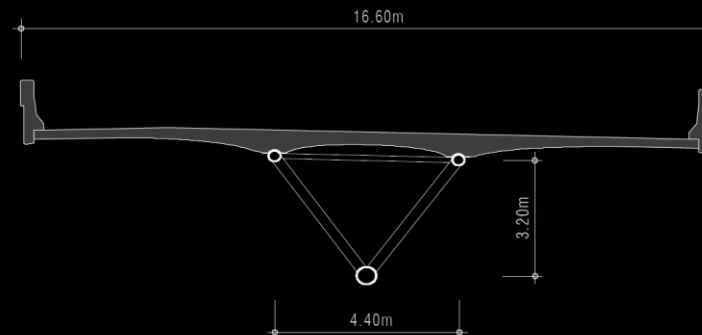
Truss bridge examples

Tubular steel trusses minimise many of the disadvantages mentioned in the previous section, and have seen a revival in the last years thanks to recent developments. Such trusses have several advantages:

- **modern sleek appearance**
- **smaller exposed surface** (compared to other trusses)
- high member inertia (slender compression members possible → **higher transparency**)

Swiss Engineer **Hans-Gerhard Dauner** (1937-2007, founder of DIC Ingénieurs at Aigle) was a pioneer in these developments.

(Note that tubular members were already used in the 19th century, e.g. Firth of Forth, but construction was highly complicated particularly for the joints).



Truss bridges – Types and examples

Truss bridge examples

The efficiency of **tubular steel-concrete composite truss bridges** can be further enhanced using concrete for both chords, combined with **prestressing**.

Mainly in France, several impressive bridges using this technology, with **external prestressing** tendons, were built in the 1990s.

Note that proper corrosion protection of the external tendons is essential for the durability of such bridges (several of the bridges built in the 1990s had to be repaired after 30 years of service due to improper grouting of the tendons).



Truss bridges – Types and examples

Truss bridge examples

An impressive example of a **tubular steel-concrete composite truss bridge** is the Bras de la Plaine bridge on La Réunion island, which was built by free cantilevering in 2002 (281 m span).

No external prestressing is provided in this bridge, but the tension diagonals are post-tensioned (and the inclined bottom chord transfers a significant part of the vertical shear forces in compression).

Notes: Massive abutments (7'250 t weight each) are required as counterweights to guarantee the stability of the bridge. The missing continuity of the bottom chord at midspan emphasises the cantilever action, but is structurally inefficient (the original design even had a hinge in the deck).



Truss bridges – Types and examples

Truss bridge examples

Concrete trusses have also been used in bridges to save weight.

Using **prefabricated ultra-high performance concrete** elements, slender truss elements are possible. (top photos: Viaduc de Glacières 1989). Nonetheless, achieving transparency is difficult.

Cast-in situ concrete trusses (with post-tensioned tension diagonals) tend to appear even heavier, making the choice of material difficult to justify: Why not use steel struts here?



Truss bridges – Types and examples

Truss bridge examples

An aesthetically convincing concrete truss bridge is the Ponte Mosteirô, by the eminent Portuguese engineer Edgar Cardoso (designer of the more famous Ponte da Arrabida).



Truss bridges – Types and examples

Other applications of trusses in bridges

Trussed members may also be used for other bridge types, such as in trussed arches (photo, see arch bridges).

Trusses are also common as **bracings and diaphragms**, and are used for **piers and pylons / towers**.

Such truss members are not treated in this chapter.



Special girder bridges

Truss bridges

Design

Truss bridges – Design

Particularities in Design – Shear deformations / slenderness

As mentioned, trusses are **very efficient structural systems**, since they closely match the optimum stringer cross-section to resist bending (see superstructure / structural efficiency).

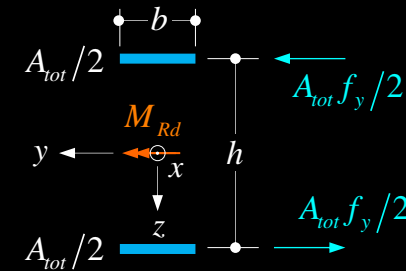
However, other than in girders with a solid web, **shear deformations** (caused by axial strains of the diagonals) are not negligible in trusses.

When **modelling a truss as a beam** without shear deformations (e.g. in preliminary design, to check the suitability of truss girders as alternative to beams in a spine or grillage model), the bending stiffness of the stringer section must be reduced accordingly (typically by about 30%).

Therefore, trusses require **more depth than solid-web girders**. For parallel chord trusses, the following slenderness ranges are common:

- simply supported truss girders: $h/L \approx 1/10 \dots 1/12$
- continuous trusses: $h/L \approx 1/12 \dots 1/16$

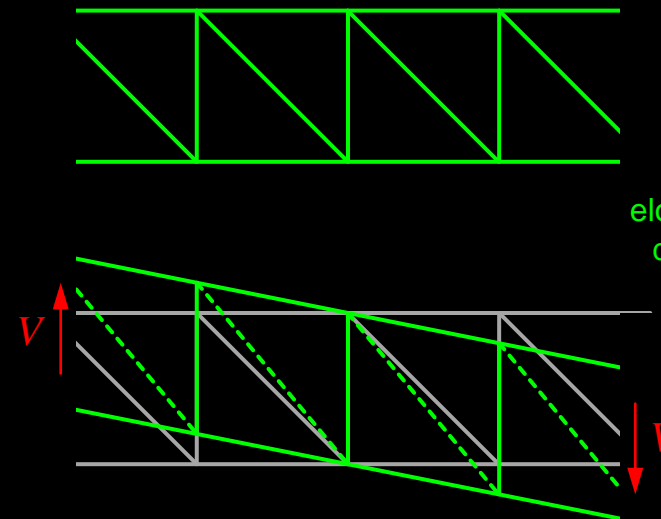
Stringer cross-section



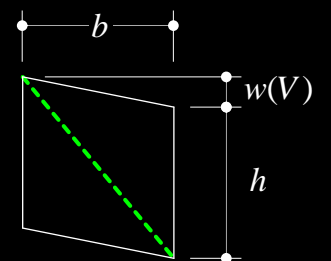
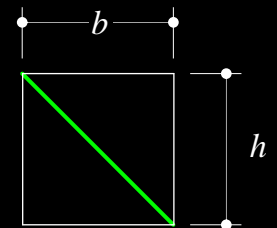
$$EI_y = 2 \frac{EA_{tot}}{2} \left(\frac{h}{2} \right)^2 = E \frac{A_{tot} h^2}{4}$$

$$M_{Rd} = \frac{f_y A_{tot}}{2} h = f_y \frac{A_{tot} h}{2}$$

Shear deformation



elongation of
diagonals



Truss bridges – Design

Particularities in Design – Structural analysis (1)

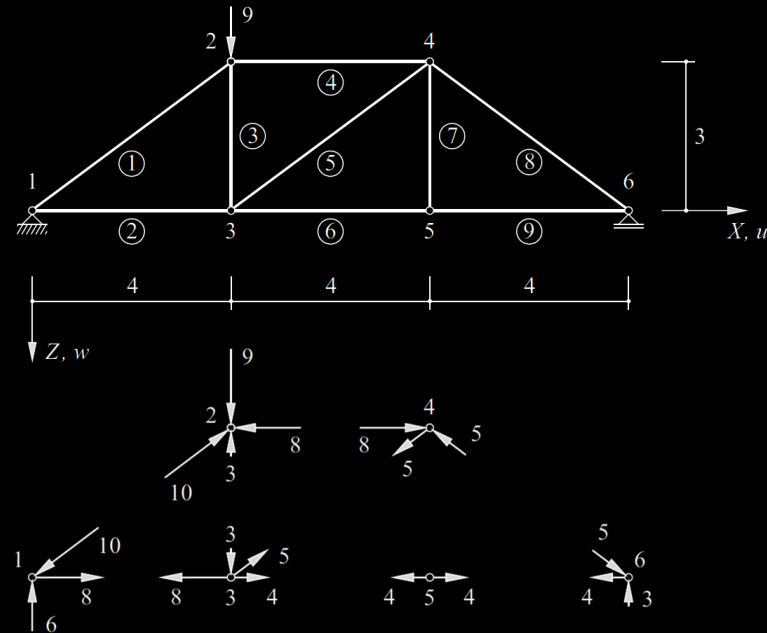
Trusses are treated in **Theory of Structures** and **Steel structures** lectures in BSc curricula (**Baustatik** and **Stahlbau I** at ETHZ). Here, some key aspects are recapitulated.

Ideal trusses transfer loads by **tension** and **compression** of truss members pin-connected at all joints. Bending moments are merely caused by loads applied to truss members between the joints.

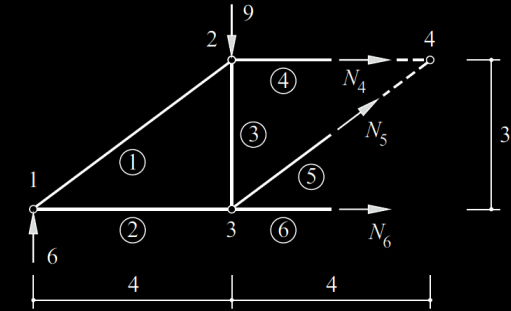
In **real trusses**, the joints are hardly ever pin-connected, causing **secondary bending moments** in the truss members. Still, the global load transfer is ensured predominantly by truss action.

The forces in isostatic ideal trusses follow from equilibrium alone. Known methods for their determination (illustrations on right) are **joint equilibrium**, **Ritter's method of sections**, and the **kinematic method**.

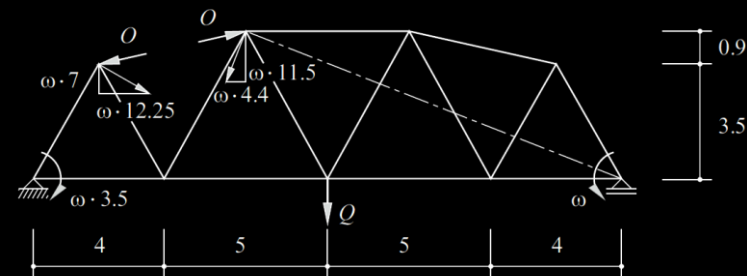
Joint equilibrium method



Ritter's method of sections



Kinematic method



[Illustrations and further information:

P. Marti, Theory of Structures, Section 11.3: Trusses]

Truss bridges – Design

Particularities in Design – Structural analysis (2)

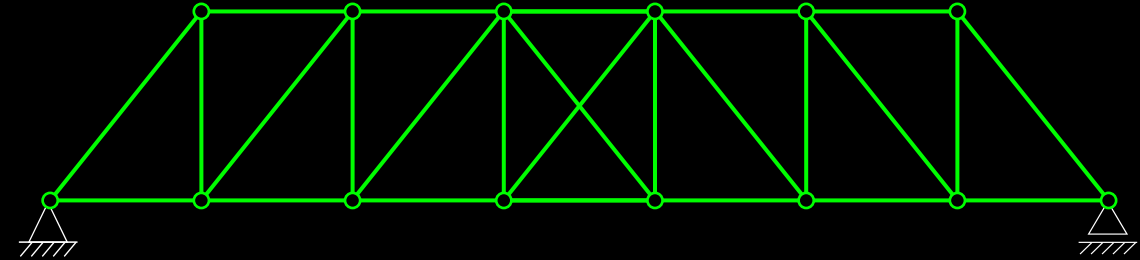
Historically, trusses were modelled as **ideal trusses** even if rigid, rather than pin-jointed, connections were provided, since this greatly simplifies the analysis (see previous slide).

The resulting **axial forces** and **deflections** closely match those of a truss with stiff connections, but **do not capture** the **secondary bending moments** caused by **joint rotations** imposed to the truss members. The latter are, however, important in bridges, where **fatigue** is relevant.

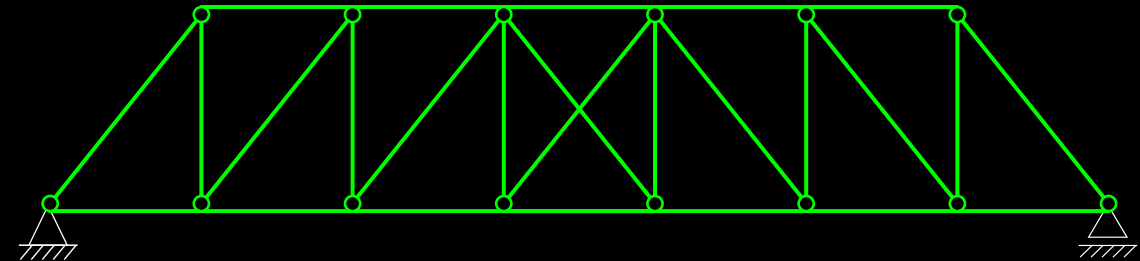
Today, using computers, it is common to analyse trusses with continuous chords, or even accounting for the **rigidity of all connections**. Secondary bending moments are thus obtained from the global analysis. Still, standards allow analysing ideal trusses and **estimating secondary bending moments** by multiplying the obtained axial stresses by **amplification factors** (typically in the range of 1.5...2) for fatigue verifications, see e.g. EN1993-1-9, Tables 4.1 and 4.2.

In any case, **eccentricities of the truss members** – causing high bending moments – should be minimised. Such eccentricities **must not be neglected** in the analysis.

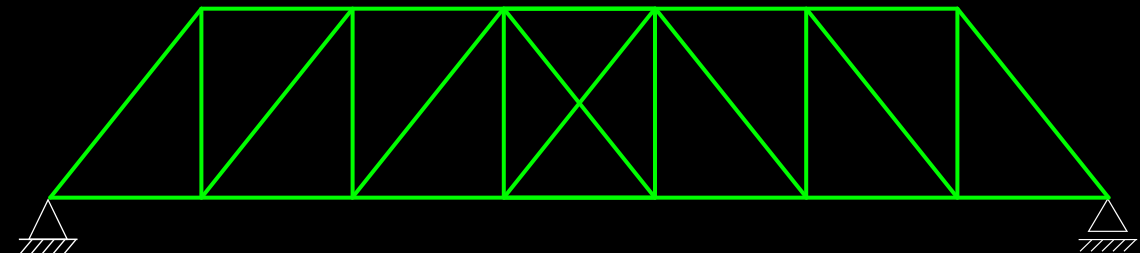
Ideal truss: All connections pin-jointed (ideal truss)
(most simple model for analysis of trusses)



Possible analysis model: Continuous chords, web members pinned
(simplified model for analysis of trusses with stiff connections)



Real truss (welded connections): All connections rigid
(accounting for secondary bending moments in all members)



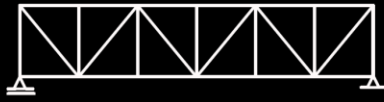
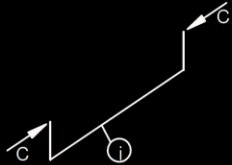
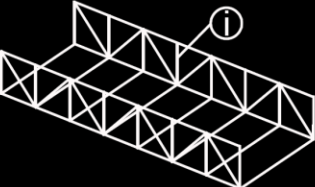
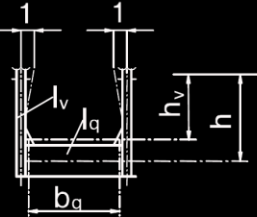
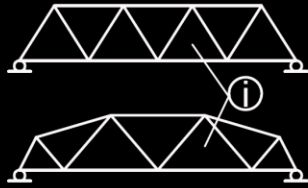
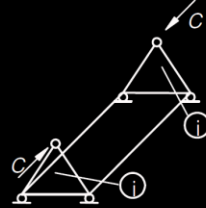
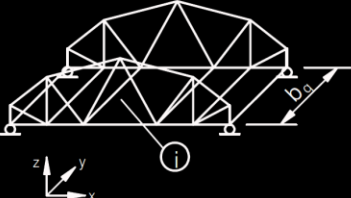
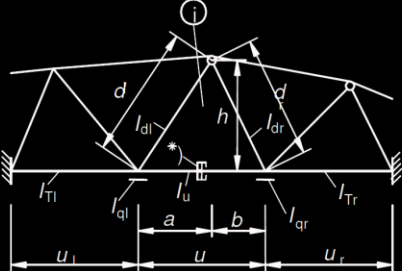
Truss bridges – Design

Particularities in Design – Required verifications

The following verifications are required when dimensioning trusses (see also lectures **Stahlbau**):

- **Cross-section resistance** and **fatigue strength** of **all truss members** (tension or compression), accounting for local instabilities of cross-sections in compression.
- **Structural safety** and **fatigue strength** of **all connections**.
- **Stability of compression members**. Unless a more refined analysis is carried out, a verification as columns is possible, assuming conservative buckling lengths of
 - ... in-plane buckling of diagonals and posts: $0.9 \cdot L$
 - ... in-plane buckling of chords: $1.0 \cdot L$
 - ... out-of-plane buckling of diagonals and post: $1.0 \cdot L$
 - ... out-of-plane buckling of chords: depending on bracing (see EN1993-2, Annex D, Table D.2 for more details)
- **Global stability of compression chords**, particularly relevant in open bridges (pony trusses). Their unbraced compression chords can be analysed as columns laterally stabilised by transverse frames (see illustration).

Excerpt from EN1993-2, Annex D, Table D.3
(global stability of unbraced compression chords)

	1	2
1	 Example of truss bridges with posts	
1a	 Modelling	 $C = \frac{EI_v}{\frac{h_v^3}{3} + \frac{h^2 b_q I_v}{2I_q}}$
2	 Example of truss bridges without posts	 2U-frame in truss bridges without posts
2a		 <p>*) torsional hinge</p>

Truss bridges – Design

Particularities in Design – Connections

The design of the **connections** is essential for the structural safety and fatigue strength of trusses. In bridges with relevant fatigue loads – particularly railway bridges – they must be carefully detailed to **minimise stress concentrations**.

Welded connections have become standard in most European countries, and hollow sections (“tubular trusses”) are preferred since they

- have a **smaller exposed surface** and a reduced tendency of accumulating debris at the joints
- are **aesthetically more appealing**, particularly if gusset plates are avoided

Corrosion protection on the inside of hollow sections is achieved by **airtight sealing**. This can hardly be achieved with bolted connections, since even small gaps (pinholes) may be sufficient to cause harmful humidity inside the cross-sections, that “breathe” under temperature variation. Therefore, **tubular trusses are less popular in North America**, where **bolted connections** are favoured.



Truss bridges – Design

Particularities in Design – Tubular truss connections

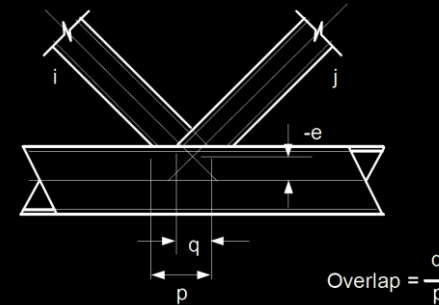
Welded connections in tubular trusses (rectangular or circular cross-section of members) may be designed using semi-empirical design equations, published by the **CIDECT**, see notes. They were derived by considering possible failure modes, differentiating between cases where the connecting members **overlap** or **provide a gap** at the chord.

In either case, **additional plates (particularly internal stiffeners) can be avoided**, even for relatively high utilisations of the connecting members (particularly for thick-walled circular chords).

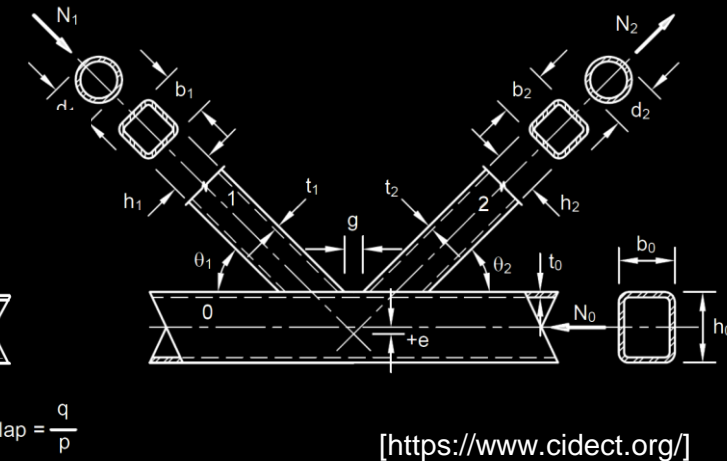
For **fatigue verifications of connections**, EN1993-1-9, Table 8.7 provides **detail categories** (36...90 MPa), to be used with the **amplification factors** accounting for secondary bending moments mentioned previously (EN1993-1-9, Tables 4.1 and 4.2).

Note **precise cutting and welding to ensure full penetration welds** (very complex geometry in circular member joints) have become available only recently. As an alternative, expensive **cast steel nodes** may be used. Thanks to the smoother transition of stiffnesses, such nodes usually provide a higher **fatigue strength**.

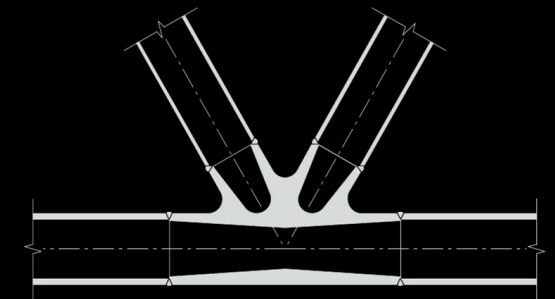
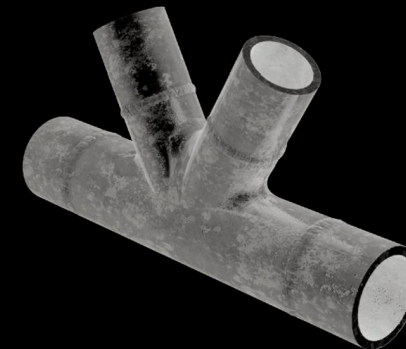
Tubular truss:
Overlap joint



Tubular truss:
Gap joint



Cast steel node



[J.P. Lebet and M.A. Hirt, Steel bridges]

Truss bridges – Design

Particularities in Design – Refined analysis methods

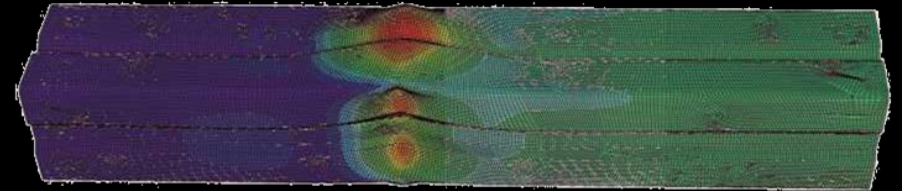
The design methods presented on the previous slides enable dimensioning truss girders in accordance with design codes. However, they contain a number of **simplifications and arbitrary assumptions**, such as:

- **buckling lengths** for compression members
- assumed **imperfections** underlying code-based verifications of plate buckling and member stability
- **amplification factors** for the estimation of secondary bending moments in fatigue verifications
- **semi-empirical design equations** for **tubular truss nodes**

Obviously, these simplifications require a certain conservatism of the design equations.

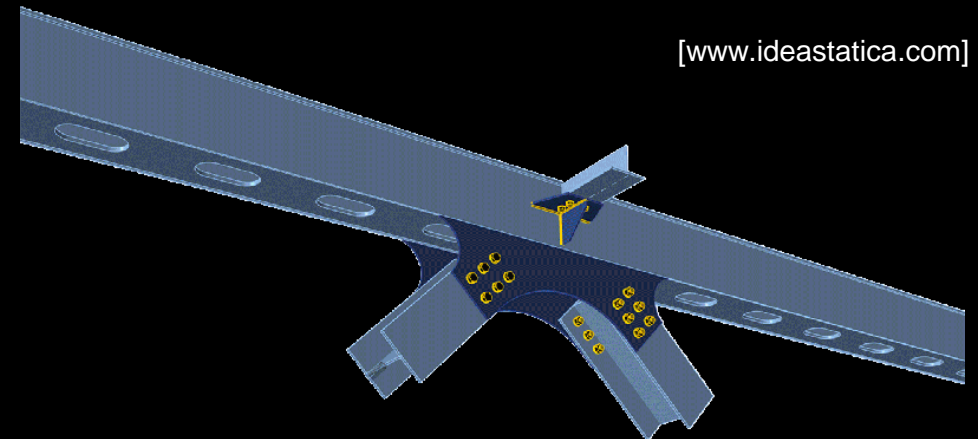
More **refined analysis methods**, mainly based on nonlinear FE-analyses, are already available today (see illustrations), and further research is ongoing (e.g. at ETH Zürich, **Chair of Steel Structures and Composite Structures**). It is expected that these methods will soon become **established in design practice**.

FE-Analysis accounting for geometrical and material nonlinearities and imperfections
(local instability of a hollow section)



[Chair of Steel Structures and Composite Structures, ETH Zürich]

Steel connection analysis based on NLFE
(commercial software IDEA StatiCa Connection)



[www.ideastatica.com]