## Advanced Structural Concrete

## Information Sheet: Nodal Zone Verification ${ }^{1}$

(101-0127-00L)

For practice, the stresses in the struts are usually assumed to be equal and the width is adapted accordingly. This leads to a biaxial uniform stress state ${ }^{2}$ : $\sigma_{1}=\sigma_{2}=f_{c}$, which simplifies the verification.

For a general nodal zone $\left(\sigma_{A} \neq \sigma_{B} \neq \sigma_{C}\right)$, the approach of the verification is explained as follows. First, the acting forces on the nodal zone need to be in equilibrium. At discontinuity lines, normal and shear stresses, $\sigma_{n}$ and $\tau_{n}$, need to be in equilibrium as well.

$$
F_{C}=\sigma_{C} \cdot b_{C}
$$

Approach:

1. Draw the Mohr's circles of each acting strut. Here $\sigma_{1}=0$ is assumed, but this does not need to be the case.
2. For each strut, find the corresponding pol $\mathrm{Q}_{i}$. The pol is the intersection of the Mohr's circle and the principal direction 3 of each strut starting at $\sigma_{1}$ (if starting at $\sigma_{3}$ it would be principal direction 1). The pol $\mathrm{Q}_{i}$ is the point on the Mohr's circle, around which stresses rotate.
3. With the help of the pol, find the point $\mathrm{S}_{i}\left(\sigma_{n i}, \tau_{n i}\right)$ which is the intersection of the Mohr's circle and the line $\mathrm{L}_{i}$, parallel to the discontinuity line of the node boundaries, passing through the corresponding pol $\mathrm{Q}_{i}$. The intersection of all $\mathrm{L}_{i}$ is the pol Q of the final Mohr's circle. All points $\mathrm{S}_{i}$ lie on the Mohr's circle of the nodal zone.
4. Finally, the Mohr's circle of the nodal zone can be drawn and the corresponding compressive stresses $\sigma_{1}$ and $\sigma_{3}$ can be read from the diagram.
5. 





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[^0]:    ${ }^{1}$ Presented in Lecture 2.1, Slide 39
    ${ }^{2}$ Often referred to as "hydrostatic" for simplicity although the stress state is not hydrostatic, because the stress perpendicular to the membrane plane is $\sigma_{3}=0$.

